

Cambridge IGCSE™

CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 4 (Extended) MARK SCHEME Maximum Mark: 120 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the February/March 2022 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of 8 printed pages.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles

Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.			
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.			
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).			
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.			
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.			

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt answers which round to
 cao correct answer only
 dep dependent
 FT follow through after error

isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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Question	Answer	Marks	Partial Marks
1(a)	$-\frac{3}{4}$ oe	2	$\mathbf{M1}$ for isolating y oe
	6	1	
1(b)(i)	$[\operatorname{grad} =] \frac{5-3}{8-4} \text{oe}$	M1	
	Substitution of (4, 3) or (8, 5) into $y = (their \ m)x + c$ or $y - y_1 = m(x - x_1)$	M1	
	$y = \frac{1}{2}x + 1$ or $2y - 6 = x - 4$ or	A1	
	2y - 10 = x - 8 leading to $2y - x = 2$ without error or omission		
1(b)(ii)	$[y=]\frac{1}{2}x+7$	2	B1 for $[y =] \frac{1}{2}x + k, \ k \neq 1$
	2		or for $[y=]jx+7, j \neq 0$
2(a)	15	1	
2(b)	47.5[0]	2	M1 for $\frac{19}{100} \times 250$ oe
2(c)	15	3	M2 for $500 + \frac{500 \times 1.5 \times y}{100} = 612.50$ oe
			or M1 for $\frac{500 \times 1.5 \times y}{100}$ oe
			or for one year's interest = 7.5[0]
2(d)(i)	13629 cao	3	B2 for 13630 or 13629
			or M1 for $20000 \times \left(1 - \frac{12}{100}\right)^3$ oe

Question	Answer	Marks	Partial Marks
2(d)(ii)	24 nfww	4	B3 for 23.4 or 23.43
			OR
			M3 $y \log \left(1 - \frac{12}{100}\right) = \log \left(\frac{1000}{20000}\right)$ oe
			or correct trials reaching 23 and 24 or good sketch indicating value between 23 and 24
			or M2 for $\left(1 - \frac{12}{100}\right)^y = \frac{1000}{20000}$ oe
			or at least 3 correct trials
			or suitable graph with $y > 1$
			or M1 for $20000 \times \left(1 - \frac{12}{100}\right)^y = 1000$ oe soi by at
			least 2 correct trials with $n > 3$
2(e)	9[.00] or 8.999 to 9.000	3	M2 for $\sqrt[10]{\frac{4673}{12000}}$
			or M1 for $12000 \times ()^{10} = 4673$
3(a)(i)	7	1	
3(a)(ii)	4	1	
3(a)(iii)	5.5	1	
3(a)(iv)	5	1	
3(b)	115.65	2	M1 for mid-values soi
3(c)	17	4	B3 for $25n + 845 = 25.4n + 838.2$ oe or better or M2 for $3 \times 5 + 11 \times 15 + n \times 25 + 19 \times 35$ = $25.4(n + 3 + 11 + 19)$ oe
			or M1 for $3\times5+11\times15+n\times25+19\times35$ oe or $25.4(n+3+11+19)$ or for correct trial with integer value of n
4(a)	[a =] 65	3	B1 for each
Γ(<i>a</i>)	$\begin{bmatrix} a - 5 & 0.5 \\ b = 1 & 8.5 \\ c = 1 & 9.5 \end{bmatrix}$	3	DI Tot Such
4(b)	[u =] 70 [v =] 30	6	B1 for each
	[w =] 80		FT 180 – their u – their v
	[x =] 20 [y =] 50 [z =] 60		FT 150 – their x – their w FT 110 – their y

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Question	Answer	Marks	Partial Marks
5(a)(i)	$4x^2 + 12x + 9$ final answer	2	B1 for three of $4x^2$, $6x$, $6x$, 9 or for correct answer seen
5(a)(ii)	4	1	FT <i>their</i> 9 – 5
5(a)(iii)	$2x + 3 = \pm \sqrt{their \ 4}$	M1	their 4 > 0
	$-2\frac{1}{2}, -\frac{1}{2}$ oe	B1	
5(b)(i)	$\frac{6}{\sqrt{w-1}}$ final answer	2	M1 for $[x=]\frac{k}{\sqrt{w-1}}$ oe
5(b)(ii)	4	1	FT only incorrect k
5(b)(iii)	$\frac{36}{x^2} + 1 \text{or} \frac{36 + x^2}{x^2} \text{or} \left(\frac{6}{x}\right)^2 + 1$ final answer	3	M1 for correct multiplication of term in w M1 for correct squaring M1 for correctly isolating w Max M2 if incorrect answer
6(a)	(5x+1)(2x-1)-7(13-x)=84 oe	M1	Correct first statement without brackets expanded
	$10x^2 - 5x + 2x - 1$	B1	
	-91 + 7x	B1	on LHS or $91 - 7x$ on RHS
	$10x^{2} + 4x - 176 = 0$ oe leading to $5x^{2} + 2x - 88 = 0$ with no errors or omissions	A1	
6(b)	(5x+22)(x-4)	2	B1 for $(5x + a)(x + b)$ with $ab = -88$ or $a + 5b = 2$ or for $5x(x - 4) + 22(x - 4)$ or for $x(5x + 22) - 4(5x + 52)$
6(c)	63	2	M1 for solving <i>their</i> factorised quadratic, allowing omission of negative root. FT $(13 - their \text{ positive root}) \times 7$ if $\frac{1}{2} < x < 13$
7(a)	Correct sketch	2	M1 for a modulus graph or for graph of $y = 4 - x^2$
7(b)	-2, 2	2	B1 for each If 0 scored, SC1 for (2, 0) and (-2, 0)

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Question	Answer	Marks	Partial Marks
7(c)	(0, 4)	1	
7(d)	1 or 2 or 3	1	
7(e)(i)	Correct sketch	1	
7(e)(ii)	1.24 or 1.236, 3.24 or 3.236	2	B1 for each or B1 for both seen e.g. $1.24 \le x \le 3.24$ or with y coords included or for 1.23 and 3.23
7(e)(iii)	Two correct regions above <i>x</i> -axis and below both graphs	2	B1 for one correct and no wrong or for one correct and one incomplete
8(a)(i)	25	1	
8(a)(ii)	-47	1	FT 3 – 2 × <i>their</i> 25
8(b)	$\frac{1}{2}$ oe	2	M1 for $2x + 1 = 3 - 2x$ or better
8(c)	7-4x final answer	2	M1 for $2(3-2x)+1$
8(d)	$\frac{3-x}{2}$ oe final answer	2	M1 for $y + 2x = 3$ or better or $\frac{y}{2} = \frac{3}{2} - x$ or $x = 3 - 2y$
8(e)	99	2	M1 for $\log(x+1) = 2(0.5) + 1$ or better
8(f)	$10^{x} - 1$	2	M1 for $10^y = x+1$ or $x = \log(y+1)$
9(a)	6.22 or 6.222 to 6.223	3	M2 for $\frac{4}{\sin 40}$ oe or M1 for $\sin 40 = \frac{4}{x}$ oe
9(b)(i)	49.5 or 49.45 to 49.46	3	M2 for [cos=] $\frac{9^2 + 10^2 - 8^2}{2.9.10}$ oe or M1 for $8^2 = 9^2 + 10^2 - 2 \times 9 \times 10$ cos()
9(b)(ii)	5.85 or 5.845 to 5.851	3	M2 for $\frac{BT}{9} = \cos(their(\mathbf{b})(\mathbf{i}))$ oe or better
			or $M1$ for CT drawn and right angle at T

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Question	Answer	Marks	Partial Marks
9(c)	21[.0] or 20.98 to 21.00	5	M2 for $\frac{12 \sin 35}{7}$ or M1 for $\frac{7}{\sin 35} = \frac{12}{\sin P}$ oe A1 for 79.5 or 79.50 to 79.51 M1 for 180 – <i>their</i> 79.5 If 0 scored, SC1 for diagram showing the two angles
10(a)	$\frac{4}{5}$ oe $\frac{7}{10}, \frac{3}{10}$ oe $\frac{9}{10}, \frac{1}{10}$ oe	3	B1 for each pair of branches
10(b)(i)	$\frac{18}{25}$ oe	2	M1 for their $\frac{4}{5} \times their \frac{9}{10}$
10(b)(ii)	$\frac{43}{50}$ oe	2	M1 for their(b)(i) + $\frac{1}{5} \times their \frac{7}{10}$ oe
10(c)(i)	$\frac{36}{43}$ oe	2	M1 for <i>their</i> (b)(ii) \times <i>p</i> = <i>their</i> (b)(i) or better
10(c)(ii)	their(b)(ii), $1 - their$ (b)(ii) oe their (c)(i), $1 - their$ (c)(i) oe $\frac{4}{7}, \frac{3}{7}$ oe	3	B1 for each pair of branches
11(a)	114.6 or 114.5 to 114.6	3	M2 for $\frac{y}{360} \times 2\pi r = 2r$ oe or M1 for $\frac{y}{360} \times 2\pi r$ oe
11(b)(i)	$\frac{x}{360} \times \pi \times 8^2 - \frac{1}{2} \times 8^2 \times \sin x = A$	M2	M1 for $\frac{x}{360} \times \pi \times 8^2$ or $\frac{1}{2} \times 8^2 \times \sin x$
11(b)(ii)	18.3 or 18.26 to 18.27	1	
11(b)(iii)	Correct sketch of curve and line	B2	B1 for correct shape of curve
	58.9 or 58.90 to 58.92	1	

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